

$D^0 - \bar{D}^0$ Mixing in FOCUS

Jonathan M. Link
 for the FOCUS Collaboration
Department of Physics, University of California, Davis, CA 95616, USA



We report on a direct measurement of the mixing parameter $y = (3.42 \pm 1.39 \pm 0.74)\%$ in the $D^0 - \bar{D}^0$ system by measuring the lifetime difference between the CP mixed final state $K^+\pi^-$ and the CP even state K^+K^- . We also present a study of the decay $D^0 \rightarrow K^+\pi^-$ based on a sample of 149 ± 31 observed events compared to $36\,760 \pm 195$ events observed in the Cabibbo favored channel $D^0 \rightarrow K^-\pi^+$. The observed branching ratio $R = (0.404 \pm 0.085 \pm 0.025)\%$ is used to obtain limits on the mixing parameters x' and y' and the doubly Cabibbo suppressed branching ratio, R_{DCS} . These studies are based on a large sample of photoproduced charm mesons from the FOCUS experiment at Fermilab (FNAL-E831).

1 Introduction

Mixing occurs because the neutral D mass eigenstates (or CP eigenstates in the limit of CP conservation) do not coincide with the flavor eigenstates D^0 and \bar{D}^0 . The mixing effects are parameterized by two dimensionless amplitudes

$$x = \frac{\Delta M}{\Gamma} \quad \text{and} \quad y = \frac{\Delta \Gamma}{2\Gamma}, \quad (1)$$

where ΔM is the mass difference between the two mass eigenstates, $\Delta \Gamma$ is the width difference and Γ is the average width. In the Standard Model, the $D^0 - \bar{D}^0$ system mixing rate ($R_{\text{mix}} = \frac{1}{2}(x^2 + y^2)$) is generally believed to be much smaller than the current experimental sensitivity¹. Nevertheless, recent measurements hint at a possible mixing effect at the edge of sensitivity. We report here on two such studies made with the FOCUS data.

The data were collected by the FOCUS Collaboration during the 1996-97 Fermilab fixed target run in the Wideband Photon beam line using an upgraded version of the E687 spectrometer². Charm particles are produced in the interaction of high energy photons ($\langle E \rangle \approx 180$ GeV) with a segmented BeO target. In the target region, charged particles are tracked by 16 layers of silicon microstrip detectors which provide excellent vertex resolution. The momentum of the charged particles is determined by measuring their deflection in two oppositely polarized, large aperture dipole magnets with five stations

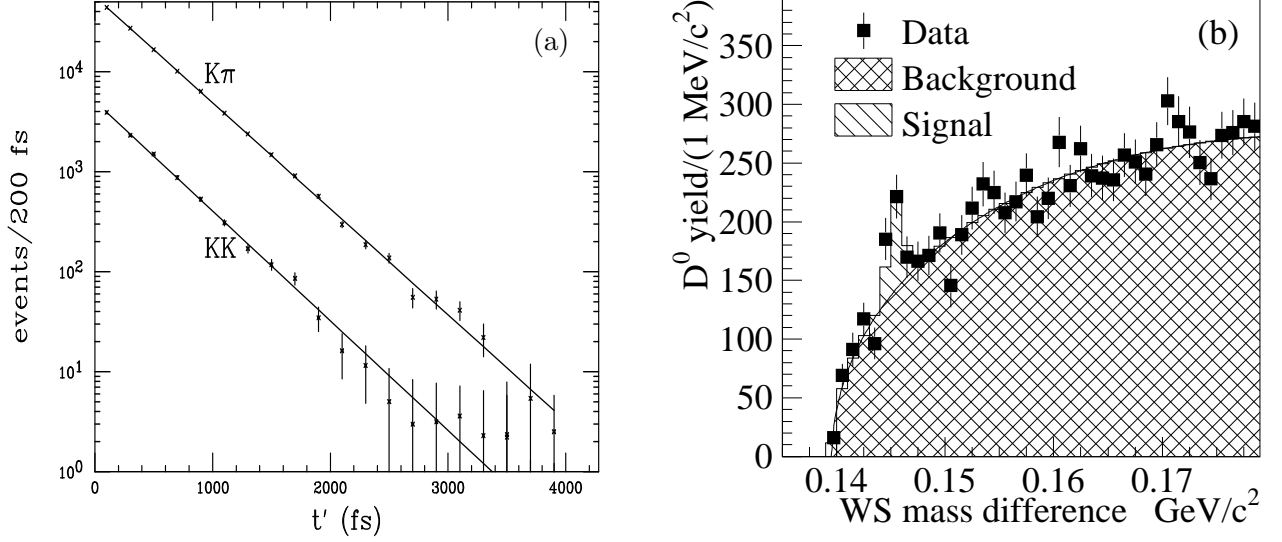


Figure 1: (a) The decay reduced proper time distribution for the selected $D^0 \rightarrow K^- \pi^+$ and $K^+ K^-$ events. The data is background subtracted and includes a small Monte Carlo correction. (b) The $D^0 \rightarrow K^+ \pi^-$ mass difference distribution with the signal and background fit contributions shown.

of multiwire proportional chambers. Particle identification is determined by three multicell threshold Čerenkov detectors, electromagnetic calorimeters, and muon counters.

2 Direct Measurement of $\Delta\Gamma$ from Lifetime Differences

By measuring and comparing the lifetime for neutral D 's decaying to final states of pure even and odd CP a direct measurement of $\Delta\Gamma$ can be made. In this study³, the final state $K^+ K^-$ is used as the CP even final state and, in the absence of a suitable CP odd candidate, the CP mixed state $K^- \pi^+$ is used. Assuming that $K^- \pi^+$ is an even mixture of CP even and CP odd the relationship between the two lifetimes and the mixing parameter y is given by

$$y = \frac{\Gamma_{CP \text{ even}} - \Gamma_{CP \text{ odd}}}{\Gamma_{CP \text{ even}} + \Gamma_{CP \text{ odd}}} = \frac{\tau(D \rightarrow K\pi)}{\tau(D \rightarrow KK)} - 1. \quad (2)$$

The lifetime distributions for the 10 331 decays to $K^+ K^-$ and 119 738 decays to $K^- \pi^+$ are shown in Fig. 1a. From exponential fits to the distributions we find $\tau(D \rightarrow KK) = 395.7 \pm 5.5 \text{ fs}$ and $\tau(D \rightarrow K\pi) = 409.2 \pm 1.3 \text{ fs}$ where the errors are statistical (systematic errors are only evaluated on the ratio). Plugging these lifetimes into Eq. (2) we obtain $y = (3.42 \pm 1.39 \pm 0.74)\%$.

3 Study of the Decay $D^0 \rightarrow K^+ \pi^-$

The process $D^0 \rightarrow K^+ \pi^-$ may occur through either a doubly Cabibbo suppressed (DCS) decay, or by D^0 mixing to \bar{D}^0 followed by the Cabibbo favored (CF) decay $\bar{D}^0 \rightarrow K^+ \pi^-$. The expected rate for the DCS decay relative to the CF decay (R_{DCS}) is approximately $\tan^4 \theta_C \simeq 0.25\%$, while Standard Model based predictions for R_{mix} range from 10^{-8} to 10^{-3} . The large uncertainty in the $D^0 - \bar{D}^0$ mixing rate is due to mixing mediated by intermediate meson states⁴ whose contributions are not calculable in perturbative QCD. Nevertheless, large cancellations among the various intermediate meson states are expected and most studies conclude that the mixing rate should be at least a couple orders of magnitude less than 10^{-3} level⁵. Also, effects from beyond the Standard Model may enhance R_{mix} .

In this study⁶, we begin by measuring the rate of $D^0 \rightarrow K^+ \pi^-$ decays relative to $D^0 \rightarrow K^- \pi^+{}^a$. The neutral D flavor is determined by requiring the decay chain $D^{+\ast} \rightarrow \pi^+ D^0 \rightarrow \pi^+ (K\pi)$. This is

^aCharge conjugate modes are implicitly included.

achieved by looking for a narrow signal at $145 \text{ MeV}/c^2$ in the mass difference between the D^* and D candidates. The mass difference distribution for $D^0 \rightarrow K^+\pi^-$ candidates is shown in Fig. 1b. We find 149 ± 31 $D^0 \rightarrow K^+\pi^-$ events compared to $36\,760 \pm 195$ decays of $D^0 \rightarrow K^-\pi^+$ for a branching ratio of $(0.404 \pm 0.085 \pm 0.025)\%$.

The time dependence of the $D^0 \rightarrow K^+\pi^-$ decays is given by

$$R(t) = \left[R_{\text{DCS}} + \sqrt{R_{\text{DCS}}} y' t + \frac{1}{4} (x'^2 + y'^2) t^2 \right] e^{-t}, \quad (3)$$

where x' and y' are phase rotations of x and y given by $x' = x \cos \delta + y \sin \delta$ and $y' = y \cos \delta - x \sin \delta$ with δ the strong force phase between the CF and DCS processes. Clearly, Eq. (3) indicates that in the case of significant mixing the measured branching ratio is dependent on the lifetime acceptance of the analysis. To account for this effect a large Monte Carlo sample of $D^0 \rightarrow K^-\pi^+$ decays is used. Each Monte Carlo event accepted in the analysis is given a weight determined by the relative probability for an event with its lifetime given by Eq. (3) divided by the probability for the same lifetime in the exponential decay rate used to generate the Monte Carlo. In this way we derive a relationship for R_{DCS} as a function of x' and y' which depends only on the measured branching ratio, and the first and second moments of the accepted lifetime distribution in the Monte Carlo. The functional dependence on x' in the experimentally allowed region is small, while the dependence on y' (shown in Fig. 2a for the case of $x' = 0$) is large. For comparison, the y' and R_{DCS} ranges from CLEO II.V⁷ and the y limit from FOCUS (discussed in Sect. 2) are also shown in this figure.

To determine limits on x' , y' and R_{DCS} , the $D \rightarrow K\pi$ data is split into high and low lifetime samples. The $D^0 \rightarrow K^+\pi^-$ branching ratio determined in each sample can be used to generate high and low lifetime curves in $y' R_{\text{DCS}}$ space like the one shown in Fig. 2a. The point where these curves cross indicates the preferred values of y' and R_{DCS} . To quantitatively determine the 95% confidence level (CL) allowed range, we integrate the likelihood for all points in the space and assign the 95% CL boundary to the high and low values beyond which the total integrated likelihood is equal to 2.5%. In determining y' (R_{DCS}) limits the value of x' is set to zero (the value of x' with greatest likelihood) and we integrate over the entire allowed range R_{DCS} (y') variable. Using this procedure we find preliminary limits of

$$\begin{aligned} -0.124 < y' < -0.006 \quad \text{and} \\ 0.43\% < R_{\text{DCS}} < 1.73\%. \end{aligned}$$

The large upper limit on R_{DCS} and large negative lower limit on y' are the result of a second crossing point of the high and low lifetime curves. This property is an unfortunate side effect of using only one lifetime split – the fitting procedure⁶ and limited statistics prevent more data splits. Nevertheless, the second crossing and its associated limits are far outside the allowed region of CLEO II.V⁷ and are also expected to be ruled out by the improved limits on x' and y' from FOCUS semileptonic mixing studies.

To determine a limit on $|x'|$ we integrate over the entire allowed range of y' and R_{DCS} obtaining the preliminary limit of

$$|x'| < 0.039.$$

We also determined a 95% CL boundary in $x' y'$ space by integrating over all allowed values of R_{DCS} and selecting the boundary line that is isometric in likelihood and contains 95% of the total likelihood. This boundary is shown in Fig. 2b. Also shown in Fig 2b are the best existing limits from the semileptonic mixing (E791⁸), lifetime differences (FOCUS) and $D^0 \rightarrow K^+\pi^-$ (CLEO II.V).

4 Conclusions

While the recent measurements in $D^0 - \overline{D}^0$ mixing do not rise to the level of a discovery, they do warrant further study. A discovery of a non-zero y at the percent level ($R_{\text{mix}} \sim 10^{-4}$) would not

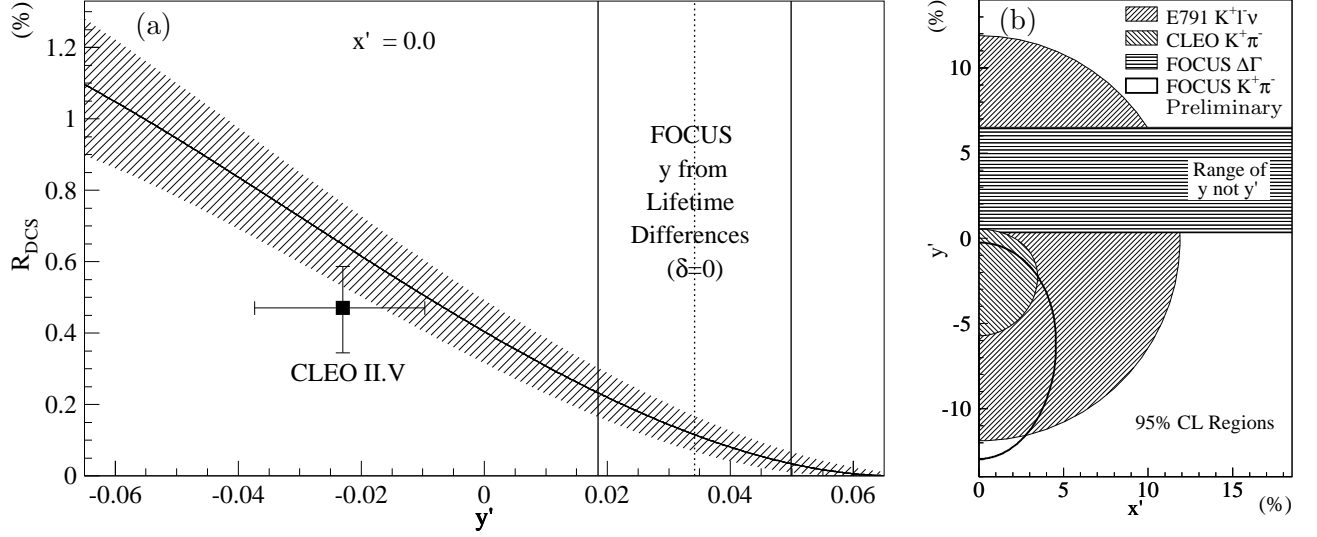


Figure 2: (a) The functional dependence of R_{DCS} on y' with $x' = 0$. Fit values of y' and R_{DCS} from CLEO II.V⁷ and the FOCUS value for y from the lifetime difference study are shown for comparison. All errors are 1σ combined statistical and systematic. (b) The 95% confidence level allowed regions for x' and y' from the E791 semileptonic study⁸, the CLEO II.V study of $D^0 \rightarrow K^+ \pi^-$ and the FOCUS study of $D^0 \rightarrow K^+ \pi^-$, and the FOCUS limits on y from lifetime differences. The direct measurement of y is only comparable to measurements on y' in the limit of strong phase $\delta = 0$. For the measurements of y' and y to be in agreement at the 1σ level requires $\delta \gtrsim \pi/4$ ⁹.

necessarily indicate new physics, but it would be unexpectedly large, and at the very least would lead to a deeper understanding of the processes involved in meson mediated mixing.

The current data from FOCUS and CLEO II.V suggest two possible scenarios. The first scenario is that there is y -like mixing at the few percent level and a large ($\sim \pi$ radians) strong phase. The second scenario is that some or all of the recent measurements are fluctuations. New measurements are required to determine which of these two possibilities is correct.

1. For a compilation of Standard Model and Non-Standard Model theoretical predictions for $D^0-\bar{D}^0$ mixing see H. N. Nelson, e-Print Archive hep-ex/9908021, (1999).
2. P. L. Frabetti *et al.*, *Nucl. Instrum. Methods A* **320**, 519 (1992).
3. J. M. Link *et al*, *Phys. Lett. B* **485**, 62 (2000).
4. L. Wolfenstein, *Phys. Lett. B* **164**, 170 (1985).
5. See for example J. F. Donoghue *et al*, *Phys. Rev. D* **33**, 179 (1986); H. Georgi, *Phys. Lett. B* **297**, 353 (1992); and T. Ohl, G. Ricciardi, E. H. Simmons, *Nucl. Phys. B* **403**, 605 (1993).
6. J. M. Link *et al*, *Phys. Rev. Lett.* **86**, 2955 (2001).
7. R. Godang *et al*, *Phys. Rev. Lett.* **84**, 5038 (2000).
8. E. M. Aitala *et al*, *Phys. Rev. Lett.* **77**, 2384 (1996).
9. S. Bergmann *et al*, *Phys. Lett. B* **486**, 418 (2000).